

Applications of Bernoulli equation

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Read notes:

(A) Bernoulli equations:

<http://www.cwru.edu/artsci/math/gurarie/classes/224/Notes/multipliers%20and%20Bernoulli.pdf>;

(B) projectile flight: <http://www.cwru.edu/artsci/math/gurarie/classes/224/Notes/flight-w-fric.pdf>.

The project has 3 parts:

- 1) Algebraic part: solve problems 1-2 on p.3 of notes (A). Derive and explain solution formulae.
- 2) Projectile motion: apply problem 2 (above), to solve problem 3, i.e. compute functions $\{v(t), \theta(t)\}$ - speed/angle
- 3) Use formulae of part 2) + integration or NDSolve in Mathematica, to compute numerically possible trajectories of projectile $(x(t), y(t))$ with initial position $(x, y) = (0, 0)$, several values of initial speed $v_0 = \{\dots\}$, and initial angle $\theta_0 = \{\dots\}$. Hint:

$$x(t) = v(t) \cdot \cos(\theta(t))$$

$$y(t) = v(t) \cdot \sin(\theta(t))$$

Plot those trajectories and compare them to 'frictionless' trajectories.

- 4) (Extra credit) Problem 4 in notes (A): logistic population with time dependent carrying capacity