Math 491 Homework 13: additional problem

Let $g: \mathbb{R} \to \mathbb{R}$ be continuous and compactly supported. Let $\varphi_t(x) = \frac{1}{\sqrt{2\pi}t}e^{-\frac{x^2}{2t^2}}$ and let $g_t = g * \varphi_t$. Give a uniform upper bound for $g_t^{(n)}$ in terms of $||g||_{\infty}$ and t.