

Prove that for a sequence of events $\{E_n\}_{n \geq 1}$,

$$\mathbb{P}[\cup_{n=1}^{\infty} E_n] \leq \sum_{n=1}^{\infty} \mathbb{P}[E_n].$$