Suppose that $X$ is uniformly distributed in $(0,1)$ and that $Y$ is the number of successes in $n$ independent trials, in which each trial succeeds with probability $X$. Find the conditional density of $X$ given that $N=k$.

